

5-3 Greatest Common Factor (GCF)

G
↓
largest

C
↓
have alike
(share)

F
↓
that goes
evenly into
another #

GCF - the largest of the common factors
of 2 or more #s

In elem. school:

14: 1 2
20: 1 2 4 5 10 20

7 14

To find GCF make a double bobsted.

$$\begin{array}{r|rr} 1.) & 3 & 27 & 45 \\ & 3 & 9 & 15 \\ & & 3 & 5 \end{array}$$

\downarrow

$\boxed{\text{GCF} = 3 \cdot 3 = 9}$

$\begin{array}{r} 3 \overline{)45} \\ \underline{-3} \\ 15 \\ \underline{-15} \\ 0 \end{array}$

Still ask yourself: what is the smallest prime # that goes evenly into both.
2, 3, 5, 7, 11, 13...

To find GCF:

Use #s on left of bobsted and multiply them.

$$\begin{array}{r|rr}
 2 & 24 & 32 \\
 \hline
 2 & 12 & 16 \\
 \hline
 2 & 6 & 8 \\
 \hline
 & 3 & 4
 \end{array}$$

$$\text{GCF} = 2 \cdot 2 \cdot 2 = 8$$

$$3.) \quad \underline{36 \quad 54}$$

$$\begin{array}{r|rr}
 2 & 36 & 54 \\
 \hline
 3 & 18 & 27 \\
 \hline
 3 & 6 & 9 \\
 \hline
 & 2 & 3
 \end{array}$$

$$\text{GCF} = 2 \cdot 3 \cdot 3 = 18$$

4.) 14 33

GCF = 1

* They don't share any other factors.

5) Triple bobsted

| | | | |
|---|----|----|----|
| 2 | 32 | 48 | 80 |
| 2 | 16 | 24 | 40 |
| 2 | 8 | 12 | 20 |
| 2 | 4 | 6 | 10 |
| | 2 | 3 | 5 |

GCF = 2 · 2 · 2 · 2 = 16
4 · 4

What if:

L
2 3 8

Must stop even though
2 + 8 have a common
factor but 3 does NOT.

$$\begin{array}{r|rr}
 6) & 24 & 48 \\
 \hline
 & 2 & 2 \\
 \hline
 & 12 & 24 \\
 \hline
 & 6 & 12 \\
 \hline
 & 3 & 6 \\
 \hline
 & 1 & 2
 \end{array}$$

$$GCF = 2 \cdot 2 \cdot 2 \cdot 3 = 24$$

$$\begin{array}{r|rrr}
 8) & 6 & 18 & 42 \\
 \hline
 & 3 & 9 & 21 \\
 \hline
 & 1 & 3 & 7
 \end{array}$$

$$GCF = 2 \cdot 3 = 6$$

$$\begin{array}{r|rr}
 7) & 32 & 48 \\
 \hline
 & 2 & 24 \\
 \hline
 & 16 & 12 \\
 \hline
 & 8 & 6 \\
 \hline
 & 4 & 3 \\
 \hline
 & 2 & 3
 \end{array}$$

$$GCF = 2 \cdot 2 \cdot 2 \cdot 2 = 16$$

$$9) \begin{array}{r|rr} 1 & 16 & 35 \end{array}$$

$$GCF = 1$$